

Introduction to Electrodynamics, 4th ed.

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Corrections to the Instructor's Solution Manual

(These corrections have been made in the current electronic version.)

(August 1, 2014)

- Page 39, Problem 2.40(b): “a” → “an”.
- Page 47, Problem 5.27(b): $Q/b \rightarrow Q/2b$.
- Page 51, Problem 2.60, replace with the following:

Problem 2.60 The initial configuration consists of a point charge q at the center, $-q$ induced on the inner surface, and $+q$ on the outer surface. What is the energy of this configuration? Imagine assembling it piece-by-piece. First bring in q and place it at the origin—this takes no work. Now bring in $-q$ and spread it over the surface at a —using the method in Prob. 2.35, this takes work $-q^2/(8\pi\epsilon_0 a)$. Finally, bring in $+q$ and spread it over the surface at b —this costs $q^2/(8\pi\epsilon_0 b)$. Thus the energy of the initial configuration is

$$W_i = -\frac{q^2}{8\pi\epsilon_0} \left(\frac{1}{a} - \frac{1}{b} \right).$$

The final configuration is a neutral shell and a distant point charge—the energy is zero. Thus the work necessary to go from the initial to the final state is

$$W = W_f - W_i = \boxed{\frac{q^2}{8\pi\epsilon_0} \left(\frac{1}{a} - \frac{1}{b} \right)}.$$

- Page 57, Problem 3.11, line 7: $W = \frac{1}{4} \dots \rightarrow W = \frac{1}{2} \dots$; in the boxed equation on that same line, $32 \rightarrow 16$.
- Page 69, Problem 3.25, first boxed equation: remove first minus sign.
- Page 99, Problem 4.22, equation following “Condition (i) says”: $s \rightarrow a$ (middle term).
- Page 154, Problem 7.37: reverse the sign of every q (a total of 10 times).
- Page 170, Problem 8.4(a), figure: remove plus and minus signs in front of the two q 's; switch axis labels x and y .
- Page 171, Problem 8.5, replace with the following:

Problem 8.5

$$(a) \mathbf{E} = -\frac{\sigma}{\epsilon_0} \hat{\mathbf{z}}, \quad \mathbf{B} = -\mu_0 \sigma v \hat{\mathbf{x}}, \quad \mathbf{g} = \epsilon_0 (\mathbf{E} \times \mathbf{B}) = \mu_0 \sigma^2 v \hat{\mathbf{y}}, \quad \mathbf{p} =$$

$$(dA) \mathbf{g} = \boxed{dA \mu_0 \sigma^2 v \hat{\mathbf{y}}}.$$

(b) (i) There is a *magnetic* force, due to the (average) magnetic field at the upper plate:

$$\mathbf{F} = q(\mathbf{u} \times \mathbf{B}) = \sigma A [(-u \hat{\mathbf{z}}) \times (-\frac{1}{2} \mu_0 \sigma v \hat{\mathbf{x}})] = \frac{1}{2} \mu_0 \sigma^2 A v u \hat{\mathbf{y}},$$

$$\mathbf{I}_1 = \int \mathbf{F} dt = \frac{1}{2} \mu_0 \sigma^2 A v \hat{\mathbf{y}} \int u dt = \frac{1}{2} d \mu_0 \sigma^2 A v \hat{\mathbf{y}}.$$

[The velocity of the patch (of area A) is actually $\mathbf{v} + \mathbf{u} = v \hat{\mathbf{y}} - u \hat{\mathbf{z}}$, but the y component produces a magnetic force in the z direction (a repulsion of the plates) which reduces their (electrical) attraction but does not deliver (horizontal) momentum to the plates.]

(ii) Meanwhile, in the space immediately above the upper plate the magnetic field drops abruptly to zero (as the plate moves past), inducing an *electric* field by Faraday's law. The magnetic field in the vicinity of the top plate (at $d(t) = d_0 - ut$) can be written, using Problem 1.46(b),

$$\mathbf{B}(z, t) = -\mu_0 \sigma v \theta(d - z) \hat{\mathbf{x}}, \quad \Rightarrow \quad \frac{\partial \mathbf{B}}{\partial t} = \mu_0 \sigma v u \delta(d - z) \hat{\mathbf{x}}.$$

In the analogy at the beginning of Section 7.2.2, the Faraday-induced electric field is just like the magnetostatic field of a surface current $\mathbf{K} = -\sigma v u \hat{\mathbf{x}}$. Referring to Eq. 5.58, then,

$$\mathbf{E}_{\text{ind}} = \begin{cases} -\frac{1}{2} \mu_0 \sigma v u \hat{\mathbf{y}}, & \text{for } z < d, \\ +\frac{1}{2} \mu_0 \sigma v u \hat{\mathbf{y}}, & \text{for } z > d. \end{cases}$$

This induced electric field exerts a force on area A of the *bottom* plate, $\mathbf{F} = (-\sigma A)(-\frac{1}{2} \mu_0 \sigma v u \hat{\mathbf{y}})$, and delivers an impulse

$$\mathbf{I}_2 = \frac{1}{2} \mu_0 \sigma^2 A v \hat{\mathbf{y}} \int u dt = \frac{1}{2} \mu_0 \sigma^2 A v d \hat{\mathbf{y}}.$$

(I dropped the subscript on d_0 , reverting to the original notation: d is the initial separation of the plates.)

The total impulse is thus $\mathbf{I} = \mathbf{I}_1 + \mathbf{I}_2 = \boxed{dA \mu_0 \sigma^2 v \hat{\mathbf{y}}}$, matching the momentum initially stored in the fields, from part (a). [I thank Michael Ligare for untangling this surprisingly subtle problem. Incidentally, there is also "hidden momentum" in the original configuration. It is not relevant here; it is (relativistic) mechanical momentum (see Example 12.13), and is delivered to the plates as they come together, so it does not affect the overall conservation of momentum.]

- Page 182, Problem 8.23, line 3: $\mathbf{H}(\nabla \times \mathbf{E}) \rightarrow \mathbf{H} \cdot (\nabla \times \mathbf{E})$.
- Page 222, Problem 10.25, downsloping arrow at upper right: in the equation for \mathbf{B} , remove the dot over the first \mathbf{J} .
- Page 227, end of line 3: $(2\sqrt{ac} + b) \rightarrow (2\sqrt{ac} + b)^{-1}$.
- Page 235, Problem 11.8: insert just before (b)

[Technically, $\dot{Q}(t)$ is discontinuous at $t = 0$, and \ddot{Q} picks up a delta function. But any *real* circuit has some (self-)inductance, which smoothes out the sudden change in \dot{Q} .]

- Page 284, Problem 12.65(b), figure: remove the two v 's (left and right sloping sides).