Name: $\qquad$

There are three questions to complete.

1. Determine the magnitude $|Z|$ of the total impedance $Z$ of the following circuit


What are the limits on your expression for $|Z|$ as the angular frequency $\omega$ approaches 0 and $\infty$ ? Can you explain these limits intuitively?
2.


Plot qualitatively the expected behavior of $V_{\text {out }}$ (or the gain) as a function of the input frequency $f\left[v_{i n}=\right.$ $\left.V_{i n} \cos (2 \pi f t)\right]$ if the black box contains
(a) a resistor,
(b) an inductor,
(c) a capacitor,
(d) an inductor and capacitor in parallel,
(e) an inductor and capacitor in series.
3.


For a black box containing a capacitor $C$ and an inductor $L$ that are connected in series, derive the resonance frequency $f_{0}$ and the FWHM (full-width-half-maximum) value $\Delta f$ of the resonance peak that is seen when plotting $\left|v_{\text {out }}\right|^{2} /\left|v_{\text {in }}\right|^{2}=V_{\text {out }}^{2} / V_{\text {in }}^{2}$. Give your answer in terms of $L, C$, and $R$.

