One of the conditions for the continuous-time lifetime utility-maximization problem is the consumption Euler equation:

$$\frac{\dot{C}(t)}{C(t)} = \frac{r(t) - \rho}{\theta}.$$

We demonstrated the following properties in the two-period model:

- If  $r > \rho$ , then the budget constraint is steeper than the indifference curve at  $C_1 = C_2$  and the household will maximize utility with  $C_2 > C_1$ .
- If  $r < \rho$ , then the budget constraint is flatter than the indifference curve at  $C_1 = C_2$  and the household will maximize utility with  $C_2 < C_1$ .
- If  $r = \rho$ , then the budget constraint is tangent to and has the same slope as the indifference curve at  $C_1 = C_2$  and the household will maximize utility with  $C_2 = C_1$ .
- If  $r \neq \rho$ , then the magnitude of the household's optimal deviation from  $C_1 = C_2$  will depend on the amount of curvature in the indifference curves, which is determined by  $1/\theta$ .
- 1. In the continuous-time setting, what conditions on the sign of  $\frac{\dot{C}}{C}$  correspond to the discrete-time outcomes:
  - a.  $C_2 > C_1$ ?
  - b.  $C_2 < C_1$ ?
  - c.  $C_2 = C_1$ ?
- 2. Show that each of the four bullet properties of the discrete-time model are also implied by the Euler equation.